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Declaration Parameters

- PVS has theory level parameters, which allow generic theories to be defined
- They are very useful, and are extensively used in the prelude and NASA libraries
- But there are situations where they are not so convenient
- The NASA libraries introduce groups with

```plaintext
groups

groups_scaf[T: TYPE, *: [T,T -> T], one: T]: THEORY
```

- Homomorphisms require two sets of parameters, hence another theory:

```plaintext
homomorphisms

homomorphism_lemmas[T1: TYPE, *: [T1,T1 -> T1], one1: T1,
T2: TYPE, o: [T2,T2 -> T2], one2: T2]: THEORY
```
A rather simple result in group theory is that homomorphisms are associative:

\[ G_1 \xrightarrow{f} G_2 \xrightarrow{g} G_3 \xrightarrow{h} G_4 \supset (h \circ g) \circ f = h \circ (g \circ f) \]

But this requires four sets of parameters, and is not included in the NASA library.
To fix this, we introduce declaration level parameters. Illustrated with yet another group theory:

```
groups

groups[G: TYPE]: THEORY
BEGIN
  group: TYPE = [# e: G,
    P: {f: [G, G -> G] | associative?(f) and forall (g: G): f(g, e) = g},
    M: {i: [G -> G] | forall (g: G): P(g, i(g)) = e} #]
END groups
```
group_morphisms

group_morphisms: THEORY
BEGIN
importing groups
homo?[G1, G2: TYPE](g1: group[G1], g2: group[G2])(f: [G1 -> G2]):
   bool =
   f(g1'e) = g2'e and
   forall (x, y: G1): f(g1'P(x, y)) = g2'P(f(x), f(y)) and
   forall (x: G1): f(g1'M(x)) = g2'M(f(x))

homo[G1, G2: TYPE](g1: group[G1], g2: group[G2]): TYPE
   = (homo?[G1, G2](g1, g2))

homo_is_assoc[G1, G2, G3, G4: TYPE]: lemma
   forall (g1: group[G1], g2: group[G2], g3: group[G3], g4: group[G4],
      f: (homo?[G1, G2](g1, g2)), g: (homo?[G2, G3](g2, g3)),
      h: (homo?[G3, G4](g3, g4))):
      h o (g o f) = (h o g) o f
END group_morphisms
PVS as Why3 Backend

- Why3 is a software verification platform
- Features an ML-style language
- Interfaces to various automated and interactive theorem provers
- Some changes introduced in Why3 made it difficult to support PVS
- In principle, this could be done in PVS by refactoring, but it is difficult
What's ahead?

PVS as Why3 Backend (cont)

Why3 to PVS

...%

% Why3 zwf_zero
zwf_zero(a:int, b:int): bool = (0 <= b) AND (a < b)

% Why3 alloc_table
alloc_table[t:TYPE]: TYPE+
...

% Why3 memory
memory[t:TYPE, v:TYPE]: TYPE+

% Why3 select
select[t:TYPE, v:TYPE+](x:memory[t, v], x1:pointer[t]): v
...

% Why3 pset
pset[t:TYPE]: TYPE+

% Why3 pset_empty
pset_empty[t:TYPE]: pset[t]
...
monad: THEORY
BEGIN
m[a: TYPE]: TYPE

return[a: TYPE]: [a -> m[a]]

>>=[a, b: TYPE](x: m[a], f: [a -> m[b]]): m[b] % infix
>>=[a, b: TYPE](x: m[a])(f: [a -> m[b]]): m[b] = x >>= f; % Curried

>>[a, b: TYPE](x: m[a])(y: m[b]): m[b] = x >>= (lambda (z: a): y);

join[a: TYPE](x: m[m[a]]): m[a] = x >>= id[m[a]]

bind_return[a, b: TYPE]: AXIOM
FORALL (x: a, f: [a -> m[b]]): (return[a](x) >>= f) = f(x)

bind_ret2[a: TYPE]: AXIOM
FORALL (x: m[a]): (x >>= return[a]) = x

END monad
Monads continued

Maybe Monad

Maybe[a: TYPE]: datatype
BEGIN
  Nothing: Nothing?
  Just(Val: a): Just?
END Maybe

maybe: THEORY
BEGIN
  IMPORTING Maybe
  IMPORTING monad
  {{ m[a: type] := Maybe[a],
    return[a: type] := Just[a],
    >>=[a, b: type](x:Maybe[a], f: [a -> Maybe[b]])
    := CASES x OF Nothing: Nothing,
      Just(y): f(y) ENDCASES }}

  f(x: int): Maybe[int] =
    IF rem(2)(x) = 0 THEN Nothing ELSE Just(2 * x) ENDIF
  g(x: int): Maybe[int] =
    IF rem(3)(x) = 0 THEN Nothing else Just(3 * x) ENDIF
  h(x: int): Maybe[int] =
    IF rem(5)(x) = 0 THEN Nothing ELSE Just(5 * x) ENDIF
  k(x: int): Maybe[int] = f(x) >>= g >>= h
END maybe

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PVS 6.0 and Beyond
PVS judgements work on types, names, numbers, and functions.

This has been extended, can now give types to arbitrary expressions under a universal quantifier:

```plaintext
expr_jdg: THEORY
BEGIN
  ej: JUDGEMENT FORALL (x: real): x*x HAS_TYPE nnreal
  f: [nnreal -> real]
  fm: FORMULA
      FORALL (y: real):
          f(f((y - 100) * (y - 100)) * f((y - 100) * (y - 100))) = 2
END expr_jdg
```
Simple ASCII text is very limiting
The Unicode standard extends this, providing a standard for representing over 110,000 characters
Both Lisp and Emacs (among many other applications) have builtin support for Unicode
In addition to display, Emacs has several input methods for conveniently inserting Unicode characters
It was relatively simple to modify the PVS parser to allow Unicode characters
What's ahead?

Unicode Demo

- `M-x list-input-methods` list available input methods
- `M-x set-input-method` selects the (buffer specific) input method
- `M-x describe-input-method` shows how to input the characters
- `C-x 8 <RET>` inputs a character by name
Unicode To Do

- Identify unary, binary, mix-fix, etc. operators to be included in the PVS grammar
- Unicode is difficult to directly use in alltt, hence needs translation
- Create a PVS input method to make it easy to insert frequently used symbols
- Backward compatibility could be supported
Cesar requested better handling of numeric values in PVS
We provided new internal representations that significantly sped up processing
This was fairly limited, and a flag had to be set to enable it
In PVS 6.0, the numeric operations (+, -, *, /) are simplified aggressively
dec :

|-------
{1} FORALL (u, s: real):
    u >= 0.78 AND s > 0 AND s < 4 AND u < 0.9 IMPLIES
    -(0.115210368 * s) - 0.101102976 * s - 0.15072 * s * u -
    0.1301216 * s * u
    - 0.018146688 * s
    - 0.4702464
    - 4 * (0.1296192 * u)
    + 0.404411904
    + 4 * (0.15072 * u)
    + 0.072586752
    + 0.1175616 * s
    + 0.101494848 * s
    + 0.015614592 * s
    + 0.1477056 * s * u
    + 0.1296192 * s * u
    >= 0
Rule? (assert)
Simplifying, rewriting, and recording with decision procedures, this simplifies to:

```
dec :
    |-------
1   FORALL (u, s: real):
    u >= 0.78 AND s > 0 AND s < 4 AND u < 0.9 IMPLIES
    13188/1953125 - 1099/312500 * (s * u) + 3297/15625000 * s +
    6594/78125 * u
    >= 0
```
What’s ahead?

- New GUI Interface
- SMT-LIB integration
- Dimension checking
- Evidential Tool Bus (ETB)
- Kernel of Truth (KoT)
We are working on a new interface to PVS
Roughly speaking, the current Emacs interface will be reimplemented as JSON
The PVS Lisp image will act as a server
Started trying to make an Eclipse interface
  very difficult—PVS is not Java
Now working on one based on wxPython
Demo
What's ahead?

SMT-LIB integration

- Yices and Yices2 are already integrated into PVS
- SMT-LIB (http://www.smtlib.org/) provides
  - standard rigorous descriptions of background theories for Satisfiability Modulo Theory (SMT) solvers,
  - common input and output languages used for these theories,
  - a large library of benchmarks
- The PVS integration provides an `smt` prover rule
- This can invoke any SMT solver that can parse SMT-LIB, (Z3, CVC4, and others)
- The advantage is that any new features provided in an SMT solver are quickly available in PVS
Dimension Checking

- DimSim is dimensional analysis extension to Simulink (with)
- It checks that Simulink blocks are dimensionally consistent, using a form of Gauss-Jordan elimination
- Paper was presented at FM 2012
- The PVS language has been extended to include dimension types, and we plan on integrating the DimSim algorithm
What's ahead?

Formal Tool Integration

- Software and hardware designs are used in many critical applications
- Formal and semi-formal tools are used in analysis and synthesis at all phases of the design lifecycle.
- A typical project integrates many diverse tools
- How do we create systematic workflows that integrates multiple tools?
- How do we make these workflows replayable?
Examples of Tool Integration

- Counterexample-guided abstraction refinement (CEGAR)
- Concolic execution uses symbolic evaluation with a SAT or SMT solver
- Bounded model checking employs a SAT or SMT solver
- Simplification using a computer algebra system such as REDUCE or QEPCAD
- Proof obligation generation for pre/post-condition specifications and refinement steps using the PVS type checker.
- Invariant generation using a range of techniques such as static analysis, templates, dynamic analysis, $k$-induction.
- Combining a verification condition generator with a range of deductive techniques for discharging proof obligations.
- Using a high-performance automated theorem prover to find an unsatisfiable core of input formulas
The main goal of ETB is the production of claims supported by arguments, where some sub-claims in the argument can be established by external tools.

The ETB should extensible with new claim forms and rules of argumentation.

The ETB should admit new external tools that interact with the ETB through an API to produce claims and generate queries.

Workflows involving external tools should be definable as scripts.

The argument produced by a completed development using the ETB should be checkable.

The ETB explicates the tools and assumptions on which an argument depends.

The ETB should be semantically neutral so that it does not exclude any tools, languages, or models.
ETB Design Choices

- Information in the ETB is in the form of queries and claims which are either atoms or negations of atoms.
- An atom is an $n$-ary predicate applied to $n$ arguments that are either data objects or variables.
- A claim is a ground (i.e., fully instantiated) atom or its negation that is asserted to hold.
- A query is a partially instantiated atom that triggers a chain of inference.
- Data objects are either JSON representations or tool or file handles.
- External tools are integrated into ETB through interpreted predicates.
- Scripts are Datalog programs defined through uninterpreted predicates.
- An ETB proof is a tree of claims where each claim follows from the subclaims by a rule of inference.
- An ETB instance is a network of server and client nodes.
Kernel of Truth

- Untrusted Frontline Verifier
- Verified Offline Verifier
- Verified Checker
- Trusted Proof Kernel

- Hints
- Certificates
- Proofs

- Verified Verifiers
- Proof generation

What's ahead?

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PVS 6.0 and Beyond
The kernel contains a reference proof system formalizing ZFC.

It also contains several verified checkers for specialized certificate formats.

If the checker validates the certificate for a claim, then there is a proof of the claim.

These certificates can be more compact than proofs.

Generating and checking certificates is easier than generating proofs.

Proof generation (including LCF) and verification are subsumed.

Verifying the checkers is (a lot) easier than verifying the inference procedures.
What's ahead?

PVS Festschrift

- PVS won the CAV award this year
- PVS was formally introduced at FME 93
- In 2014 it turns 21 (old enough to drink)
- We are planning a Festschrift for 2014:
  - Still in the conceptual stages
  - Have multiple AFM meetings:
    - in Europe at FM (formerly FME)
    - in the US at CAV
    - possibly in Asia
- Papers would be a mix of historical origins, definitive papers, and applications
- **Hope to see you there!**