



Formal Verification of Large Software Systems

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Motivation

■ Software Systems

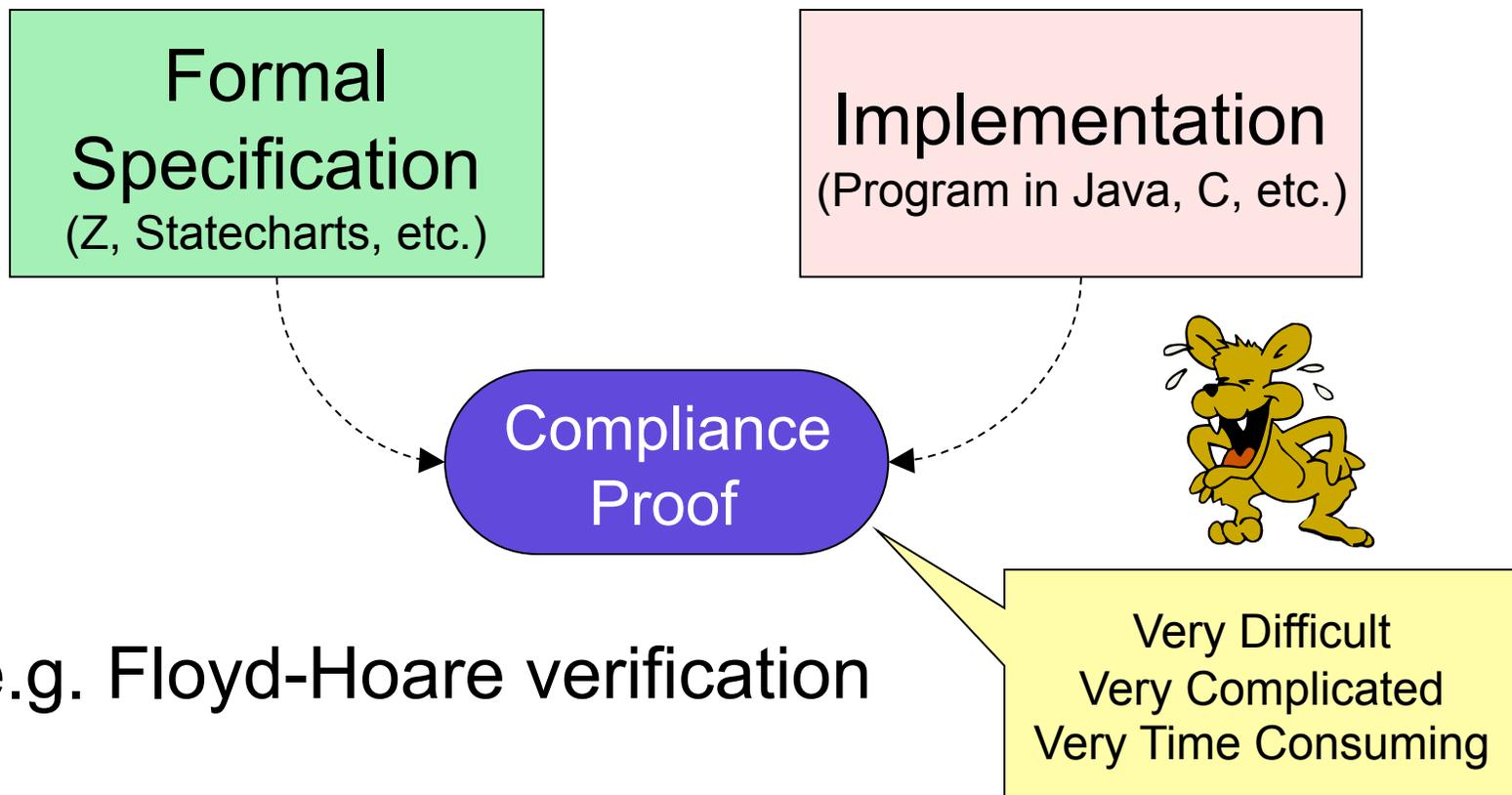
- Safety and security are critical concerns
- Formal verification highly desirable



- Increasing size and complexity
- Current approaches not widely applied
- Formal verification needs to become routine

Proofs in Traditional Verification

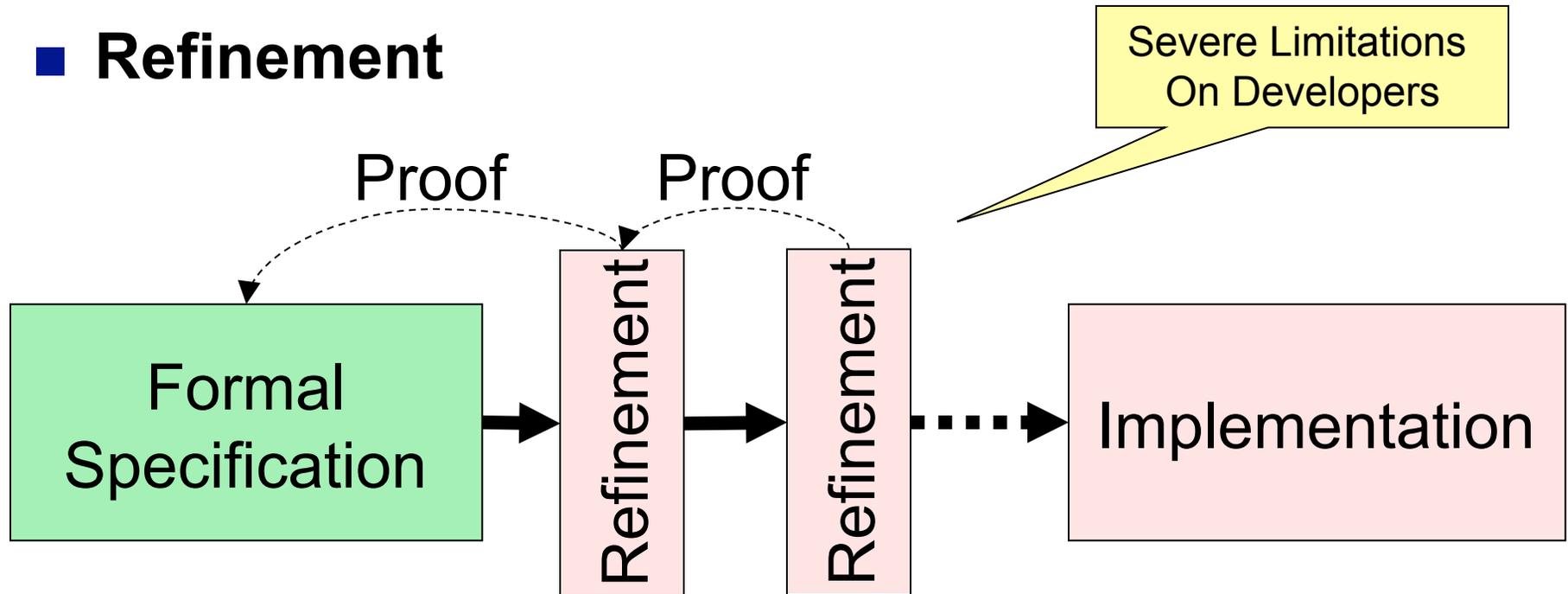
■ Correctness Proof



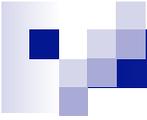
■ e.g. Floyd-Hoare verification

Proofs in Traditional Verification

■ Refinement



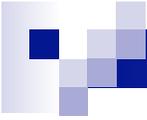
■ e.g. B Method



Our Goal

- Focus on ***functional correctness***
- More **practical** proof structure
- Goals:
 - Relevant
 - Scalable
 - Accessible
 - Efficient

This Is Strictly a
Pragmatic Issue



Our Goal

- Focus on ***functional correctness***
- More **practical** proof structure
 - Relevant
 - Benefit from formal verification
 - Scalable
 - Applicable to larger systems
 - Accessible
 - Routine usage
 - Efficient
 - Acceptable time and resource

This Is Strictly a
Pragmatic Issue

"Standard" development process

Semantics restricted to be implementable

Semantics-preserving transformations to reduce verification complexity

Conventional Development

Original Specification

Implementation

Reverse Synthesis

Implication Proof

Update or complete source-code annotations

Annotation

Verification Refactoring

Extracted Specification

Specification Extraction

Implementation Proof

Refactored Implementation

Mechanical proof to show implication

Automatic Floyd/Hoare verification

Mechanical translation to specification language

Proof Process

Structural Matching Hypothesis

- High-level structure of a specification retained in the implementation
 - Specification: contain design information
 - Implementation: often similar in structure, at least in partial
 - Save design effort
 - More maintainable
- e.g. Z schema  System operation
- e.g. model-based specifications: states & operations

```
state: TYPE = [# a: int, b: int #]  
foo(st: state) : state
```



```
type state is  
  record  
    a: Integer;  
    b: Integer;  
  end record;
```

```
procedure foo(st: in out state);  
  --# derives st from st;
```

Structural Matching Hypothesis

High-level structure of specification tends to be retained in the implementation

- Example: Model-based specifications states & operations:

Z schema  System operation

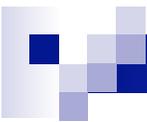
```
state: TYPE = [# a: int, b: int #]
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```
type state is
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    b: Integer;
  end record;

procedure foo(st: in out state);
--# derives st from st;
```

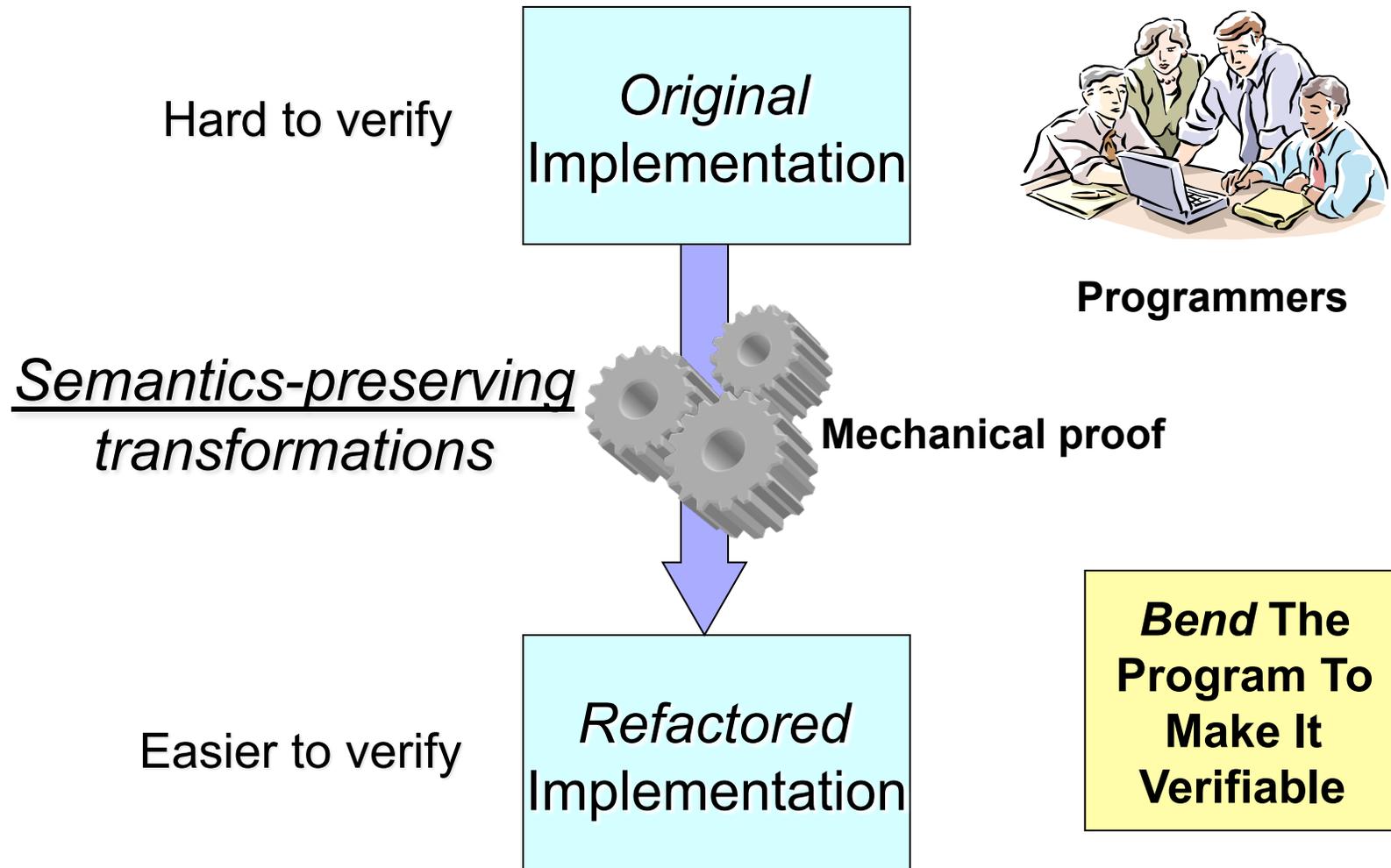
- Advantages to implementer:
 - Save design effort, more maintainable



Proof by Parts

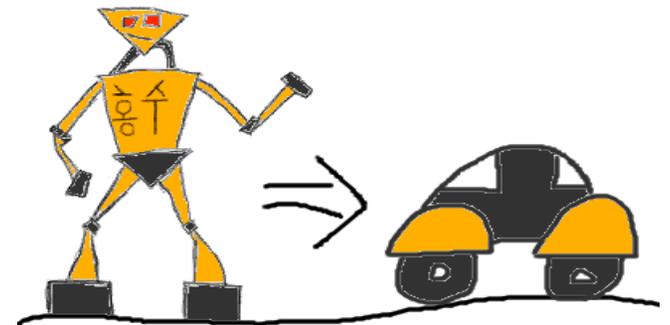
- Implementation I, Specification S: $I \Rightarrow S$
 - $\text{pre}(S) \Rightarrow \text{pre}(I) \wedge \text{post}(I) \Rightarrow \text{post}(S)$
 - Weakens the pre-condition
 - Decreases non-determinism
- Rely on reverse synthesis:
 - Break into two proofs
 - Make implication proof between two abstract specifications
- Rely on structural matching hypothesis:
 - Pairs of matching elements: types, states, operations
 - Implication lemma for each *distinct* element

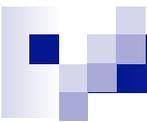
Verification Refactoring



Verification Refactoring

- Transform implementation to facilitate verification
- Simplify verification conditions
- Reduce complexity introduced in design
 - Careful treatment of special cases
 - Compact data structures
 - Efficient algorithms
 - Complexity in the control- and data-flow
- Support proof by parts
- Align the structure
 - Matches extracted specification & original specification
 - Allows an efficient overall proof structure





Metric Analysis

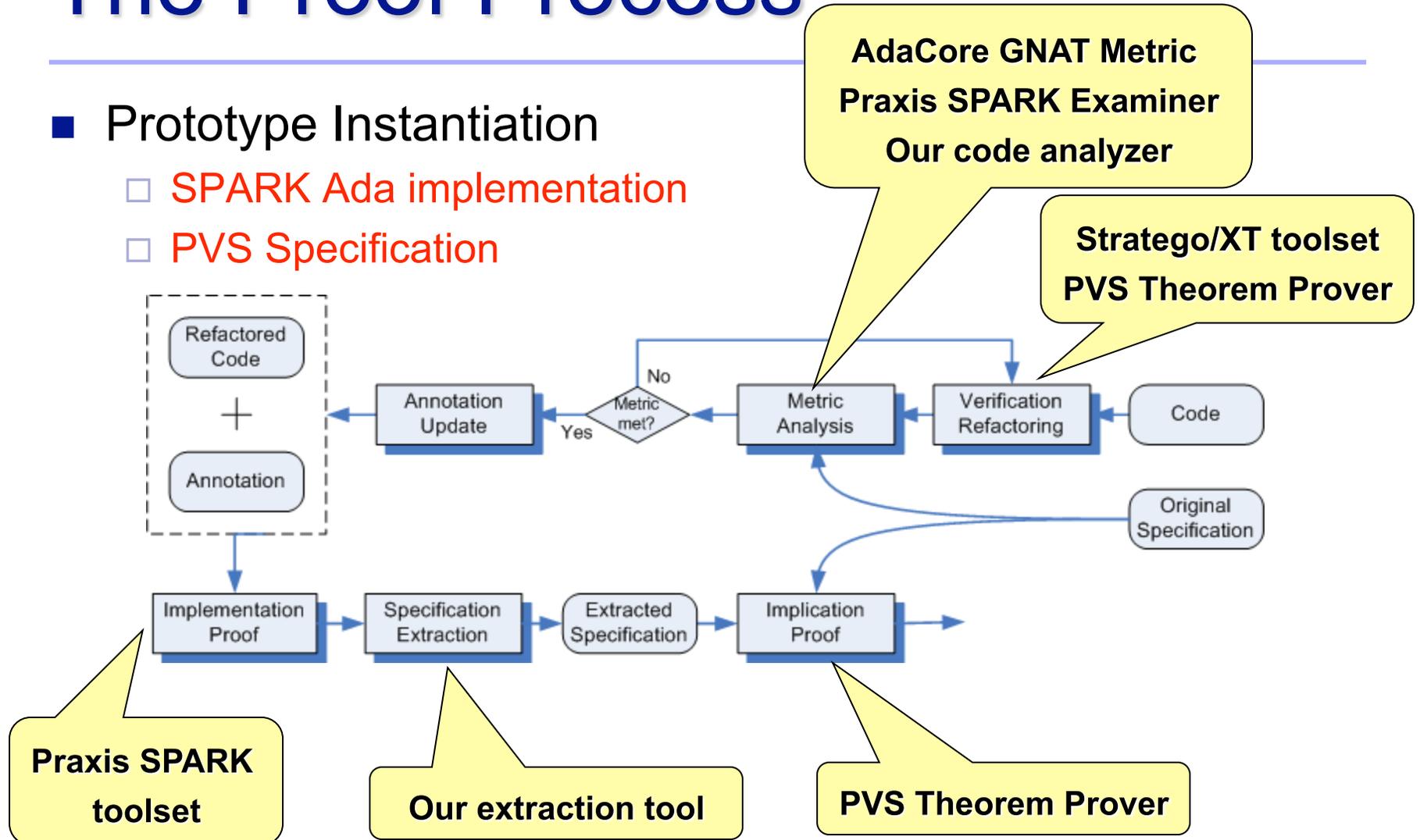
- A hybrid of metrics for review:
 - *Element metrics*
 - Lines of code, number of statements, construct nesting level, etc.
 - *Complexity metrics*
 - McCabe cyclomatic complexity, loop nesting level, etc.
 - *Verification condition metrics*
 - Number and size of VCs, machine time to analyze the VCs, etc.
 - ***Specification matching metric***
 - Support proof by parts
 - Summary of the structures of the original and the extracted specifications
 - Visually inspected and evaluated match-ratio

- Indicate likely difficulty of proof

The Proof Process

- Prototype Instantiation

- SPARK Ada implementation
- PVS Specification



Specification Extraction

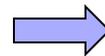
■ Extraction from annotation

- Proved pre- and post-condition annotation
- Introduced as a proved lemma
- Leave out the unrelated implementation details
 - Correctness of the output but not actual algorithm

□ e.g.

```
type state is
  record
    a: Integer;
    b: Integer;
  end record;
```

```
procedure foo(st: in out state)
--# derives st from st;
--# pre st.a = 0;
--# post st = st~[a => 1];
is
begin
  -- procedure body
  ...
end foo;
```



```
state: TYPE = [# a: int, b: int #]
```

```
foo_pre(st: state): bool = (st`a = 0)
```

```
foo_post(st_, st: state): bool =
  (st = st_ WITH [`a := 1])
```

```
foo(st: state): state
```

```
foo: LEMMA FORALL (st: state):
  foo_pre(st) => foo_post(st,
  foo(st))
```

Specification Extraction

- Direct extraction from code

- No proper annotation
- Not helpful in abstracting out details

- e.g.

```
procedure foo(st: in out state)
is
begin
  foo1(st);
  st.a = 1;
  foo2(st);
end foo;
```

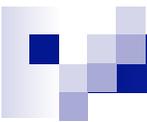


```
foo(st: state): state =
  LET st1 = foo1(st) IN
  LET st2 = st1 WITH [`a := 1] IN
  LET st3 = foo2(st2) IN
  st3
```

- Skeleton extraction

- Lightweight version, structure only
- Facilitate metric analysis

- Component Reuse & Model Synthesis



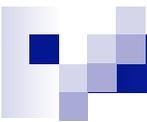
Implication Proof

- Implication ***lemma*** for each pair of matching elements
- Implication ***theorem*** as conjunction of all lemmas

- *Type Lemma*
 - Type refinement

- *State Lemma*
 - State match
 - State initialization

- *Operation Lemma*
 - Applicability
 - Correctness



Implication Proof

■ Operation Lemma

- Set up according to behavior subtyping

- Applicability

- The extracted operation has a weaker pre-condition
- Applicable whenever the original operation is

```
FORALL st:  
  Pre_org(R(st)) => Pre_ext(st)
```

- Correctness

- The extracted operation has a stronger post-condition if applicable
- When applicable, generate allowed output of the original operation

```
FORALL st1, st2 | st2 = f(st1):  
  Post_ext(st2) AND pre_org(R(st1)) => post_org(R(st2))
```

Evaluation

■ Target: The *Tokeneer ID Station*



Developers

- Hypothetical secure enclave protection software
 - Defined by NSA as security challenge problem
 - Developed by Praxis High Integrity Systems

Z
Specification
(117 pages)

SPARK Ada
Implementation
(9939 lines)

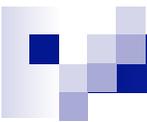
PVS
Specification
(2336 lines)



Verifiers

■ Scenario:

- Public available artifacts (developed by others)
- Non-trivial application
- Several thousand lines long
- In a domain requiring high assurance
- Focus on **functional proof**



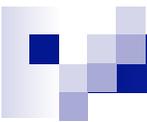
Tokeneer Proof

- Proof: correctness of functionality:
 - Different from Praxis' correctness by construction proof
- Structural matching hypothesis:
 - Upon review:
 - Source code structure resembled specification closely
 - Skeleton extraction:
 - Structure match ratio 74.7%
- Verification refactoring:
 - Sufficiently similar to proceed without major refactoring
- Specification extraction:
 - 5622 lines of PVS extracted automatically

Tokeneer Proof

- Implementation Proof
 - Pre- / post-condition annotations, freedom from run-time exceptions
 - SPARK toolset: Over 2600 VCs generated, 95% VCs discharged automatically
- Implication Proof
 - Matching elements identified straightforwardly
 - Can be partly automatically suggested by names
 - Over 300 implication lemmas
 - Most TCCs discharged automatically
 - 10% of the lemmas discharged automatically
 - 90% required straightforward human intervention
 - expansion of function definitions
 - introduction of type predicates
 - application of extensionality
 - etc.
- Complete Proof
 - Identified mismatches that were documented design decisions





Conclusion

■ Proof by parts

- Focus on proof of functional correctness
- Designed to scale for large software systems
 - Demonstrated on a program several thousand lines long
- Does not impose restrictions on software development
- Also eases the location of implementation defects
- Infeasible if structural matching hypothesis does not hold
 - Verification refactoring can help align the structures

Questions?

